

# Matching for Credit: Implications for Econometric Analysis and Market Design

Thilo Klein

Centre for European Economic Research (ZEW) Mannheim

January 25, 2018

# Motivation: one-sided matching

Economists often observe data on interactions...

- which students teamed up in study groups;
- which characters formed entrepreneurial teams;
- which firms merged with each other.

Example 1: Rules on inter-cultural mix of an organisation

- 1 **direct effect**: Do communication problems outweigh the synergies within mixed teams?
- 2 direct effect is net of **sorting bias**: Are open-minded workers more likely to sort into mixed teams?
- 3 **participation effect**: Does the applicant pool change if the management stipulates mixed teams?



# Motivation: microcredit

## Lending to the poor without any financial securities

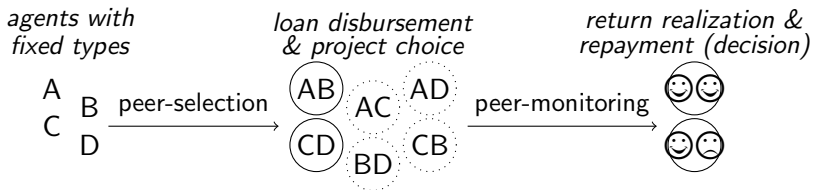
- 2005: UN declared “International Year of Microcredit”
- 2006: Muhammad Yunus awarded Nobel Peace Prize
- 2010: First IPO of Indian microfinance institute SKS

## Enabled by innovation in contract design

- high screening, monitoring and enforcement costs
- joint-liability delegates responsibilities to self-selected groups
- But: groups avoid liability payments if projects fail concurrently

→ Is there a role for rules to diversify groups?

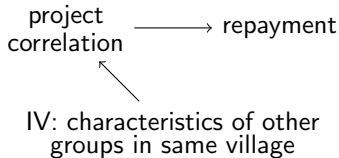
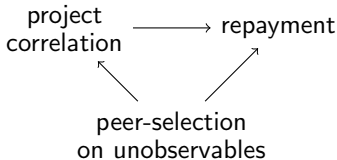
## Example 2: Group lending (sequence of events)



### Market design question

Should MFIs prevent the grouping together of borrowers who are exposed to similar income shocks?

### Econometric problem and identification strategy



# Contributions

## Empirical work

- ambiguous empirical results: three studies find a negative effect and one – Ahlin/Townsend (2007) – finds the opposite
- sorting bias is well recognised in literature, but experimental studies fail to estimate policy-relevant parameters
- current paper is the first to simultaneously account for group selection and outcomes with credible exclusion restriction

## Theoretical models of joint-liability lending

- this is not a paper that considers what is the optimal contract. Instead, it informs the optimal design of market rules
- it develops the key trade-offs of conflicting predictions of asymmetric information models in Ahlin/Townsend (2007) and Ghatak (2000)

# Outline

- 1 Motivation
- 2 One-sided matching
  - Model set-up
  - Participation effect
- 3 Empirical strategy
  - Direct effect
  - Monte-Carlo simulations
- 4 Results
  - Data
  - Direct effect

# Model set-up (Stiglitz/Weiss 1981)

## Agents and projects

- risk neutral agents with no collateral invest in ind. projects
- inherently different prob. of success,  $p \in [\underline{p}, 1]$
- same expected returns, i.e.  $p \cdot y(p) = E$
- project covariation modelled by adding/subtracting const.  $\bar{\epsilon}$

	$j$ succeeds ( $p_j$ )	$j$ fails ( $1 - p_j$ )
$i$ succeeds ( $p_i$ )	$p_i p_j + \bar{\epsilon}$	$p_i(1 - p_j) - \bar{\epsilon}$
$i$ fails ( $1 - p_i$ )	$(1 - p_i)p_j - \bar{\epsilon}$	$(1 - p_i)(1 - p_j) + \bar{\epsilon}$

## Information and contract

- agents know each others' risk-type,  $p$ , but lender does not
- pooling contract with fixed interest payment,  $r$
- liability payment,  $q$ , is due if group member's project fails

→ Expected payoff:  $u_i = E - rp_i - q[p_i(1 - p_j) - \bar{\epsilon}]$



## Participation effect

Expected payoff of agent  $i$  matching with agent  $j$

$$\bullet u_i = \underbrace{E}_{\text{return}} - \underbrace{rp_i}_{\text{interest}} - \underbrace{q[p_i(1 - p_j) - \bar{\epsilon}]}_{\text{joint liability}}$$

Matching on risk type (Gatak 1999) and credit rationing

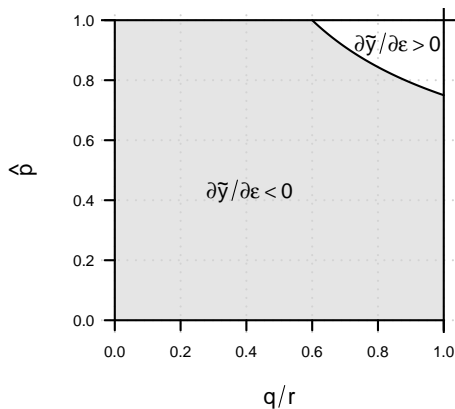
- homogenous matching in equilibrium, thus  $p_i = p_j$
- cut-off type  $\hat{p}$  solves participation equation with equality
 
$$E - r\hat{p} - q[\hat{p}(1 - \hat{p}) - \bar{\epsilon}] = \bar{u}.$$
- i.e. credit is rationed for agents with projects safer than  $\hat{p}$ .

Repayment effects of increased project covariation  $\bar{\epsilon}$

- + draws safer types into the portfolio (Ahlin/Townsend 2007)
- but overall, does not offset loss of liability payment (this paper)

## Participation effect (cont'd)

Conditions for positive repayment effect of project correlation for uniform distribution of risk type



$\rightarrow \partial \tilde{y} / \partial \epsilon < 0$  if  $\hat{p} < 0.75$  or  $q/r < 0.6$

# Outline

- 1 Motivation
- 2 One-sided matching
  - Model set-up
  - Participation effect
- 3 Empirical strategy**
  - Direct effect
  - Monte-Carlo simulations
- 4 Results
  - Data
  - Direct effect

## Empirical strategy: direct effect

**Sorting bias:** Let a group's expected repayment be given as

$$Y_{ij} = 1[Y^* > c] \quad \text{with: } Y_{ij}^* = \beta_0 + \beta_1 \cdot \gamma_i \gamma_j + \delta \cdot (d_i + d_j) + \zeta_{ij}. \quad (1)$$

If  $(d_i + d_j)$  is unobserved, then  $\hat{\beta}_1^{ols}$  is biased upwards when  $\delta < 0$  and  $\text{cov}(\gamma_i \gamma_j, (d_i + d_j)) < 0$ .

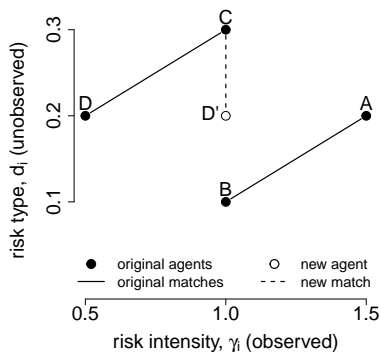
**Empirical strategy:** Estimate unobserved group risk as a residual in the matching model

$$D_{ij} = 1[V_{ij} \in \Gamma_\mu] \quad \text{with: } V_{ij} = \alpha \cdot \gamma_i \gamma_j + (d_i + d_j)$$

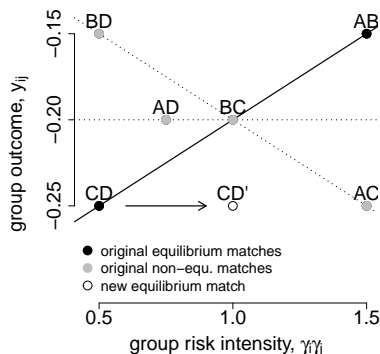
and selection-correct repayment equation (1).

# Identification

(a) One-sided matching and exogenous variation



(b) Regression bias and resolution with exogenous variation

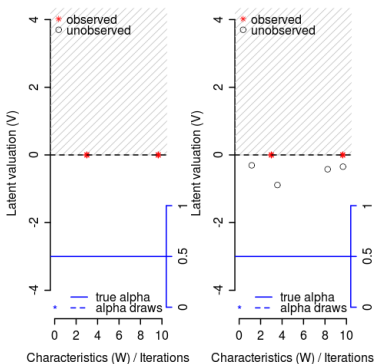


→ Recall:  $Y_{ij} = \delta \cdot (d_i + d_j)$

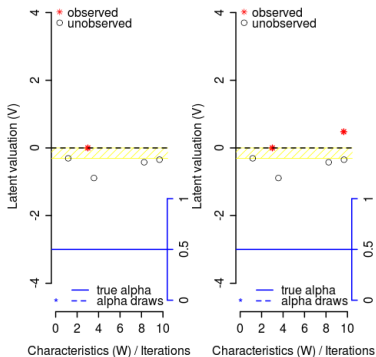
# Estimation: Gibbs sampler for matching model

## Matching estimator (illustrated)

(a) Draw match valuations for unobserved groups

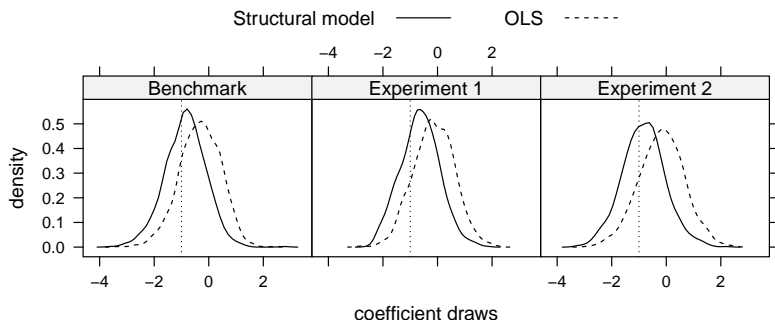


(b) Draw match valuations for 1st observed group



# Monte-Carlo simulations

Posterior distributions of parameters for 40 two-group markets based on 1,000 draws. True slope parameter  $\beta = -1$ .



**Benchmark:** All members (6/6); all counterfactuals (922/922)

**Experiment 1:** 5 randomly sampled group members

**Experiment 2:** 250 randomly sampled counterfactual groups

# Outline

- 1 Motivation
- 2 One-sided matching
  - Model set-up
  - Participation effect
- 3 Empirical strategy
  - Direct effect
  - Monte-Carlo simulations
- 4 Results
  - Data
  - Direct effect



# Data

## Robert M. Townsend (2000) data on BAAC groups in Thailand

- BAAC is largest lender in rural Thailand
- 39 villages from 2 regions randomly sampled with stratification
- in every village, as many BAAC groups as possible were surveyed, up to two: 68 groups and 316 borrowers in total

## Variables

- $wst$ : coincidence of economically bad years
- $p_i p_j$ : interaction of groups' project success probability, with

$$p_i = \frac{E_i - L_i}{H_i - L_i}$$

based on borrower  $i$ 's expected income in an average year  $E_i$ , good year  $H_i$  and bad year  $L_i$ .

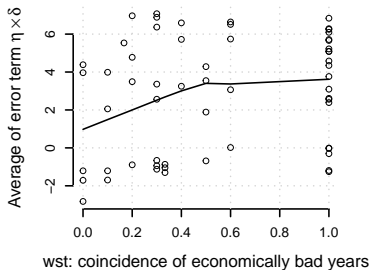
	Probit 1	Probit 2	Structural
<b>Outcome equation</b>			
<i>Response: repayment_outcome = 1 if group never repaid late</i>			
<i>Risk type</i>			
- success_prob $p_i$	-	+1	+1
- success_prob_int $p_i p_j$	-	0.238 (1.606)	1.571 (1.813)
<i>Project covariation</i>			
- same_worst_year <i>wst</i>	0.170 (0.289)	-0.015 (0.219)	-0.586 (0.243)**
<i>Controls</i>			
- loan_size	-	0.263 (0.421)	0.970 (0.362)**
- loan_size_sqrd	-	-0.050 (0.088)	-0.187 (0.080)*
- ln(group_age)	-0.040 (0.054)	-0.116 (0.161)	-0.395 (0.109)***
- FE for two-group vill's	YES	YES	YES
	N=68	N=68	N=68
<b>Matching equation</b>			
<i>Response: group observability indicator = 1 if group is observed</i>			
<i>Risk type</i>			
- success_prob_int $p_i p_j$	-	-	-0.778 (0.992)
<i>Project covariation</i>			
- same_worst_year <i>wst</i>	-	-	0.356 (0.119)**
	-	-	N=5,342
<b>Variance</b>			
covariance $\delta$	-	-	0.512 (0.127)***

*S.E. in parentheses; one-sided significance at 0.1, 1, 5, 10% denoted by \*\*\*, \*\*, \*, and .*

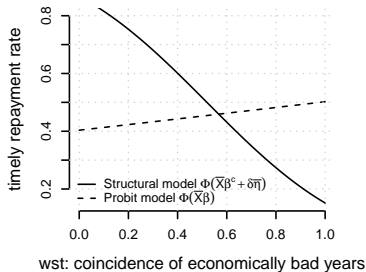
# Direct effect: Probit vs. structural model

## Decomposition of sorting bias and direct effect.

(a) Equilibrium groups with high project covariation have better unobservables



(b) Probit predictions (dashed line) comprise direct effect (straight line) and sorting bias



→ A one s.d. increase in *wst* has two opposing effects.

1. drop in prob. of timely payment by 22 percentage points (p.p.).
2. groups have observables and unobs. that are on avg. 28 p.p. safer.

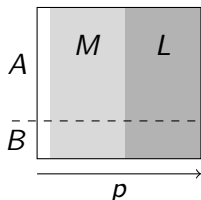
# Direct effect: Assumptions

## Preferences

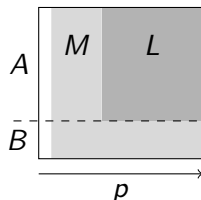
- **aligned** in risk type  $p \in [0.5, 1)$ , in that borrowers always prefer a safer partner (irrespective of their own type), but also
- **assortative** in exposure type  $s \in \{A, B\}$ , in that borrowers only value partners of their own type.

Matching on risk type (horizontal axis) and exposure type

(a) Aligned preferences I



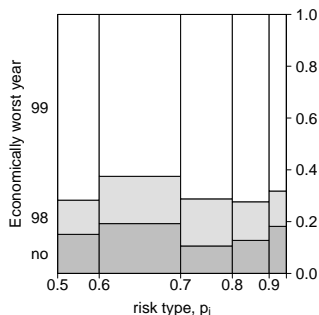
(b) Aligned preferences II



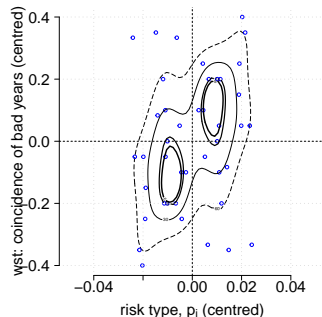
## Direct effect: Assumptions (cont'd)

## Validation of assumptions underlying the matching model

(a) Assumption of independence  $p \perp s$



(b) Assumption of aligned preferences



# Conclusion

## Empirical analysis of endogenous groups

- distinction between participation and direct effect allows test of ex-ante versus ex-post mechanisms
- useful where evaluation of adverse selection models requires that moral hazard effects are not in force, and vice versa
- method is implemented in R package [matchingMarkets](#)

## Economic theories of microfinance

- theories must consider that matching also takes place on other dimensions – such as common shocks – with adverse effects

## Microfinance practice

- group lending clients – about 65 million worldwide – could benefit if lenders were to actively diversify borrower groups