

Contest Quiz 4

Question Sheet

In this quiz we will review concepts of linear regression covered in lectures 4 and 5.

NOTE: Please round your results to *two decimal places*.

EXAMPLE: If your unrounded solution is 0.13897439, drop all decimal places except the first three. This leaves you with 0.138. If the third decimal place is 5 or above (as is the case here), round up. This gives 0.14.

Question 1: Simple linear regression

- (i) Consider the linear model $Y_i = \beta_0 + \beta_1 X_i + u_i$. The variance of Y_i is given by
- (a) $\beta_0^2 + \beta_1^2 \text{var}(X_i) + \text{var}(u_i)$.
 - (b) the variance of u_i .
 - (c) $\beta_1^2 \text{var}(X_i) + \text{var}(u_i)$.
 - (d) the variance of the residuals.
- (ii) The sample average of the OLS residuals is
- (a) some positive number since OLS uses squares.
 - (b) zero.
 - (c) unobservable since the population regression function is unknown.
 - (d) dependent on whether the explanatory variable is mostly positive or negative.
- (iii) The slope estimator, $\hat{\beta}_1$, has a smaller standard error, other things equal, if
- (a) there is more variation in the explanatory variable, X .
 - (b) there is a large variance of the error term, u .
 - (c) the sample size is smaller.
 - (d) the intercept, β_0 , is small.
- (iv) The regression R^2 is a measure of
- (a) whether or not X causes Y .
 - (b) the goodness of fit of your regression line.
 - (c) whether or not $ESS > TSS$.
 - (d) the square of the determinant of R .

- (v) To decide whether or not the slope coefficient is large or small,
 - (a) you should analyse the economic importance of a given increase in X .
 - (b) the slope coefficient must be larger than one.
 - (c) the slope coefficient must be statistically significant.
 - (d) you should change the scale of the X variable if the coefficient appears to be too small.
- (vi) Multiplying the dependent variable by 100 and the explanatory variable by 100,000 leaves the
 - (a) OLS estimate of the slope the same.
 - (b) OLS estimate of the intercept the same.
 - (c) regression R^2 the same.
 - (d) variance of the OLS estimators the same.
- (vii) In which of the following relationships does the intercept have a real-world interpretation?
 - (a) the relationship between the change in the unemployment rate and the growth rate of real GDP (“Okun’s Law”)
 - (b) the demand for coffee and its price
 - (c) test scores and class-size
 - (d) weight and height of individuals
- (viii) Changing the units of measurement, e.g. measuring test scores in 100s, will do all of the following EXCEPT for changing the
 - (a) residuals
 - (b) numerical value of the slope estimate
 - (c) interpretation of the effect that a change in X has on the change in Y
 - (d) numerical value of the intercept

Question 2: Hypothesis tests and confidence intervals

- (i) When estimating a demand function for a good where quantity demanded is a linear function of the price, you should
 - (a) not include an intercept because the price of the good is never zero.
 - (b) use a one-sided alternative hypothesis to check the influence of price on quantity.
 - (c) use a two-sided alternative hypothesis to check the influence of price on quantity.
 - (d) reject the idea that price determines demand unless the coefficient is at least 1.96.
- (ii) The confidence interval for the sample regression function slope
 - (a) can be used to conduct a test about a hypothesized population regression function slope.
 - (b) can be used to compare the value of the slope relative to that of the intercept.
 - (c) adds and subtracts 1.96 from the slope.
 - (d) allows you to make statements about the economic importance of your estimate.

- (iii) Under the least squares assumptions (zero conditional mean for the error term, X_i and Y_i being *i.i.d.*, and X_i and u_i having finite fourth moments), the OLS estimator for the slope and intercept
- (a) has an exact normal distribution for $n > 15$.
 - (b) is BLUE.
 - (c) has a normal distribution even in small samples.
 - (d) is unbiased.
- (iv) Consider the following regression line: $\widehat{TestScore} = 698.9 - 2.28 * STR$. You are told that the t -statistic on the slope coefficient is 4.38. What is the standard error of the slope coefficient?
- (v) The construction of the t -statistic for a one- and a two-sided hypothesis
- (a) depends on the critical value from the appropriate distribution.
 - (b) is the same.
 - (c) is different since the critical value must be 1.645 for the one-sided hypothesis, but 1.96 for the two-sided hypothesis (using a 5% probability for the Type I error).
 - (d) uses ± 1.96 for the two-sided test, but only $+1.96$ for the one-sided test.
- (vi) The only difference between a one- and two-sided hypothesis test is
- (a) the null hypothesis.
 - (b) dependent on the sample size n .
 - (c) the sign of the slope coefficient.
 - (d) how you interpret the t -statistic.
- (vii) Using 143 observations, assume that you had estimated a simple regression function and that your estimate for the slope was 0.04, with a standard error of 0.01. You want to test whether or not the estimate is statistically significant. Which of the following possible decisions is the only correct one:
- (a) you decide that the coefficient is small and hence most likely is zero in the population
 - (b) the slope is statistically significant since it is four standard errors away from zero
 - (c) the response of Y given a change in X must be economically important since it is statistically significant
 - (d) since the slope is very small, so must be the regression R^2 .

Question 3: Multiple regression models

- (i) In the multiple regression model, the adjusted R^2 , \bar{R}^2
- (a) cannot be negative.
 - (b) will never be greater than the regression R^2 .
 - (c) equals the square of the correlation coefficient $r_{Y\hat{Y}}$.
 - (d) cannot decrease when an additional explanatory variable is added.

- (ii) Under imperfect multicollinearity
- (a) the OLS estimator cannot be computed.
 - (b) two or more of the regressors are highly correlated.
 - (c) the OLS estimator is biased even in samples of $n > 100$.
 - (d) the error terms are highly, but not perfectly, correlated.
- (iii) When there are omitted variables in the regression, which are determinants of the dependent variable, then
- (a) you cannot measure the effect of the omitted variable, but the estimator of your included variable(s) is (are) unaffected.
 - (b) this has no effect on the estimator of your included variable because the other variable is not included.
 - (c) this will always bias the OLS estimator of the included variable.
 - (d) the OLS estimator is biased if the omitted variable is correlated with the included variable.
- (iv) Imagine you regressed earnings of individuals on a constant, a binary variable (*Male*) which takes on the value 1 for males and is 0 otherwise, and another binary variable (*Female*) which takes on the value 1 for females and is 0 otherwise. Because females typically earn less than males, you would expect
- (a) the coefficient for *Male* to have a positive sign, and for *Female* a negative sign.
 - (b) both coefficients to be the same distance from the constant, one above and the other below.
 - (c) none of the OLS estimators to exist because there is perfect multicollinearity.
 - (d) this to yield a difference in means statistic.
- (v) When you have an omitted variable problem, the assumption that $E(u_i X_i) = 0$ is violated. This implies that
- (a) the sum of the residuals is no longer zero.
 - (b) there is another estimator called weighted least squares, which is BLUE.
 - (c) the sum of the residuals times any of the explanatory variables is no longer zero.
 - (d) the OLS estimator is no longer consistent.
- (vi) In the multiple regression model you estimate the effect on Y_i of a unit change in one of the X_i while holding all other regressors constant. This
- (a) makes little sense, because in the real world all other variables change.
 - (b) corresponds to the economic principle of *mutatis mutandis*.
 - (c) leaves the formula for the coefficient in the single explanatory variable case unaffected.
 - (d) corresponds to taking a partial derivative in mathematics.

- (vii) You have to worry about perfect multicollinearity in the multiple regression model because
- many economic variables are perfectly correlated.
 - the OLS estimator is no longer BLUE.
 - the OLS estimator cannot be computed in this situation.
 - in real life, economic variables change together all the time.
- (viii) The intercept in the multiple regression model
- should be excluded if one explanatory variable has negative values.
 - determines the height of the regression line.
 - should be excluded because the population regression function does not go through the origin.
 - is statistically significant if it is larger than 1.96.
- (ix) The following OLS assumption is most likely violated by omitted variables bias:
- $E(u_i|X_i) = 0$
 - $(X_i, Y_i), i = 1, \dots, n$ are *i.i.d* draws from their joint distribution
 - there are no outliers for X_i, u_i
 - there is heteroskedasticity
- (x) In multiple regression, the R^2 increases whenever a regressor is
- added unless the coefficient on the added regressor is exactly zero.
 - added.
 - added unless there is heteroskedasticity.
 - greater than 1.96 in absolute value.
- (xi) Consider the following multiple regression models (a) to (d) below. $DFemme = 1$ if the individual is a female, and is zero otherwise; $DMale$ is a binary variable which takes on the value one if the individual is male, and is zero otherwise; $DMarried$ is a binary variable which is unity for married individuals and is zero otherwise, and $DSingle$ is $(1 - DMarried)$. Regressing weekly earnings ($Earn$) on a set of explanatory variables, you will experience perfect multicollinearity in the following cases unless:
- $\widehat{Earn}_i = \hat{\beta}_0 + \hat{\beta}_1 DFemme + \hat{\beta}_2 Dmale + \hat{\beta}_3 X_{3i}$
 - $\widehat{Earn}_i = \hat{\beta}_0 + \hat{\beta}_1 DMarried + \hat{\beta}_2 DSingle + \hat{\beta}_3 X_{3i}$
 - $\widehat{Earn}_i = \hat{\beta}_0 + \hat{\beta}_1 DFemme + \hat{\beta}_3 X_{3i}$
 - $\widehat{Earn}_i = \hat{\beta}_1 DFemme + \hat{\beta}_2 Dmale + \hat{\beta}_3 DMarried + \hat{\beta}_4 DSingle + \hat{\beta}_5 X_{3i}$
- (xii) Consider the multiple regression model with two regressors X_1 and X_2 , where both variables are determinants of the dependent variable. When omitting X_2 from the regression, then there will be omitted variable bias for $\hat{\beta}_1$
- if X_1 and X_2 are correlated
 - always
 - if X_2 is measured in percentages
 - if X_2 is a dummy variable

- (xiii) Consider the multiple regression model with two regressors X_1 and X_2 , where both variables are determinants of the dependent variable. You first regress Y on X_1 only and find no relationship. However when regressing Y on X_1 and X_2 , the slope coefficient $\hat{\beta}_1$ pertaining to X_1 changes by a large amount. This suggests that your first regression suffers from
- (a) heteroskedasticity
 - (b) perfect multicollinearity
 - (c) omitted variable bias
 - (d) dummy variable trap
- (xiv) Imperfect multicollinearity
- (a) implies that it will be difficult to estimate precisely one or more of the partial effects using the data at hand
 - (b) violates one of the four Least Squares assumptions in the multiple regression model
 - (c) means that you cannot estimate the effect of at least one of the X s on Y
 - (d) suggests that a standard spreadsheet program does not have enough power to estimate the multiple regression model

Question 4: Hypothesis tests in multiple regression

- (i) The following linear hypothesis can be tested using the F -test with the exception of
- (a) $\beta_2 = 1$ and $\beta_3 = \beta_4/\beta_5$.
 - (b) $\beta_2 = 0$.
 - (c) $\beta_1 + \beta_2 = 1$ and $\beta_3 = -2\beta_4$.
 - (d) $\beta_0 = \beta_1$ and $\beta_1 = 0$.
- (ii) When testing joint hypothesis, you should
- (a) use t -statistics for each hypothesis and reject the null hypothesis if all of the restrictions fail.
 - (b) use the F -statistic and reject all the hypothesis if the statistic exceeds the critical value.
 - (c) use t -statistics for each hypothesis and reject the null hypothesis once the statistic exceeds the critical value for a single hypothesis.
 - (d) use the F -statistics and reject at least one of the hypothesis if the statistic exceeds the critical value.
- (iii) The overall regression F -statistic tests the null hypothesis that
- (a) all slope coefficients are zero.
 - (b) all slope coefficients and the intercept are zero.
 - (c) the intercept in the regression and at least one, but not all, of the slope coefficients is zero.
 - (d) the slope coefficient of the variable of interest is zero, but that the other slope coefficients are not.

- (iv) For a single restriction, the F -statistic
- is the square root of the t -statistic.
 - has a critical value of 1.96.
 - will be negative.
 - is the square of the t -statistic.
- (v) Let $R^2_{unrestricted}$ and $R^2_{restricted}$ be 0.4366 and 0.4149 respectively. The difference between the unrestricted and the restricted model is that you have imposed two restrictions. **That is, there are 3 regressors (excluding the intercept) in the unrestricted model and 1 regressor in the restricted model.** There are 420 observations. What is the F -statistic in this case?
- (vi) If you reject a joint null hypothesis using the F -test in a multiple hypothesis setting, then
- a series of t -tests may or may not give you the same conclusion.
 - the regression is always significant.
 - all of the hypotheses are always simultaneously rejected.
 - the F -statistic must be negative.
- (vii) A 95% confidence set for two or more coefficients is a set that contains
- the sample values of these coefficients in 95% of randomly drawn samples.
 - integer values only.
 - the same values as the 95% confidence intervals constructed for the coefficients.
 - the population values of these coefficients in 95% of randomly drawn samples.
- (viii) When testing the null hypothesis that two regression slopes are zero simultaneously, then you cannot reject the null hypothesis at the 5% level, if the confidence ellipse contains the point
- $(-1.96, 1.96)$.
 - $(0, 1.96)$.
 - $(0, 0)$.
 - $(1.96^2, 1.96^2)$.
- (ix) All of the following are true, with the exception of one condition:
- a high R^2 or \bar{R}^2 does not mean that the regressors are a true cause of the dependent variable.
 - a high R^2 or \bar{R}^2 does not mean that there is no omitted variable bias.
 - a high R^2 or \bar{R}^2 always means that an added variable is statistically significant.
 - a high R^2 or \bar{R}^2 does not necessarily mean that you have the most appropriate set of regressors.
- (x) Consider a regression with two variables, in which X_{1i} is the variable of interest and X_{2i} is the control variable. Conditional mean independence requires
- $E(u_i|X_{1i}, X_{2i}) = E(u_i|X_{2i})$
 - $E(u_i|X_{1i}, X_{2i}) = E(u_i|X_{1i})$
 - $E(u_i|X_{1i}) = E(u_i|X_{2i})$
 - $E(u_i) = E(u_i|X_{2i})$
- (xi) What is the critical value of $F_{4,\infty}$ at the 5% significance level?